

Chapter 36

SOLVING FOR VARIABLES

Often, we are not given a number to substitute for the variable. This is when we must "solve for the unknown," or "solve for x ."



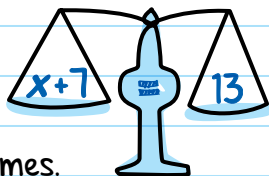
Solving an equation is like asking, "Which value makes this equation true?"

In order to do so, we must **ISOLATE THE VARIABLE** on one side of the equal sign.

EXAMPLE: $x + 7 = 13$

In order to isolate the variable (x) on one side of the equal sign, we must:

1. Think of an equation as a scale, with the $=$ sign as the middle. You *must* keep the scale balanced at all times.



2. Ask yourself, "What is happening to this variable?"
In this case, 7 is being added to the variable.

3. So, how do we get the variable alone? We use **INVERSE OPERATIONS** on both sides of the equation.
What is the inverse of adding 7? Subtracting 7.

WHEN YOU SEE THE WORD **INVERSE**,
THINK ABOUT OPPOSITES!

$$x + 7 = 13$$

$$x + \cancel{7} - \cancel{7} = 13 - 7$$

$$x = 6$$

(We subtract 7 from both sides
to keep the equation balanced.)

CHECK YOUR WORK

$$x + 7 = 13$$

$$6 + 7 = 13$$

$$13 = 13 \quad \checkmark$$

Check your work by
plugging your answer into
the original equation.

Inverse is just another word for *opposite*. Here's a quick
rundown of all the operations and their inverse operations:

OPERATION

INVERSE

Addition \longrightarrow Subtraction

Subtraction \longrightarrow Addition

Multiplication \longrightarrow Division

Division \longrightarrow Multiplication

Squaring (exponent of 2) \longrightarrow Square root ($\sqrt{\quad}$)

Cubing (exponent of 3) \longrightarrow Cube root ($\sqrt[3]{\quad}$)